

Relating Inflationary Predictions to the Modulus Mass

Koushik Dutta

Theory Division, Saha Institute

TCGCA IV, IISER-Kolkata

September, 2015

In collaboration with
ANSHUMAN MAHARANA (HRI, Allahabad)

Phys.Rev. D91 (2015) 4, 043503

arXiv:1409.7037[hep-ph]

KUMAR DAS (Saha Institute)
ANSHUMAN MAHARANA (HRI, Allahabad)

arXiv:1506.05745[hep-ph]

some ongoing work ..

Prologue

'Modular Cosmology'



post-inflationary
moduli mass

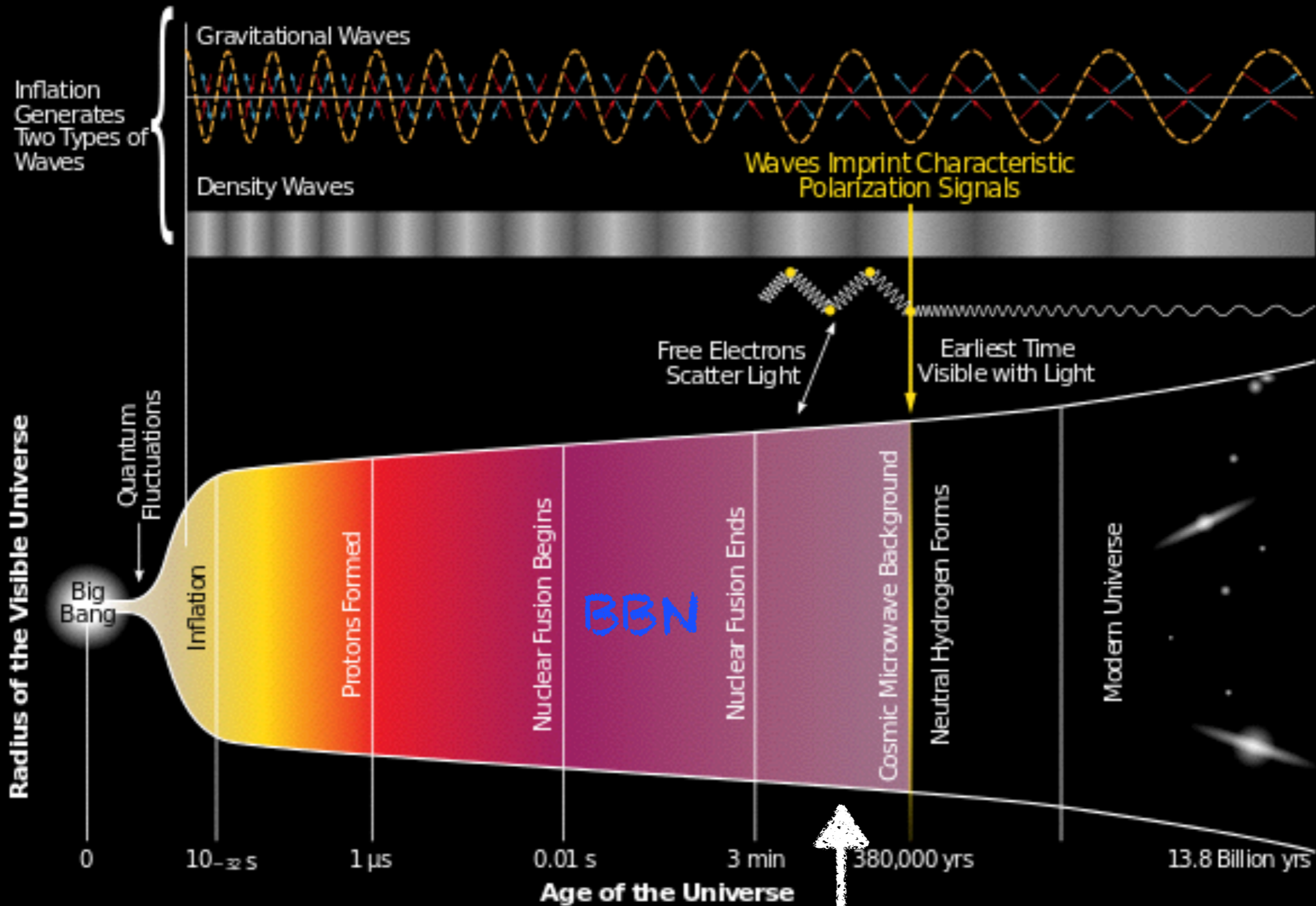
$$Y = \hat{\varphi}/M_{Pl} \sim 1$$

Outline

- Inflation 101
- Cosmology with moduli
- Constraint on moduli mass/inflation
- Implications ..

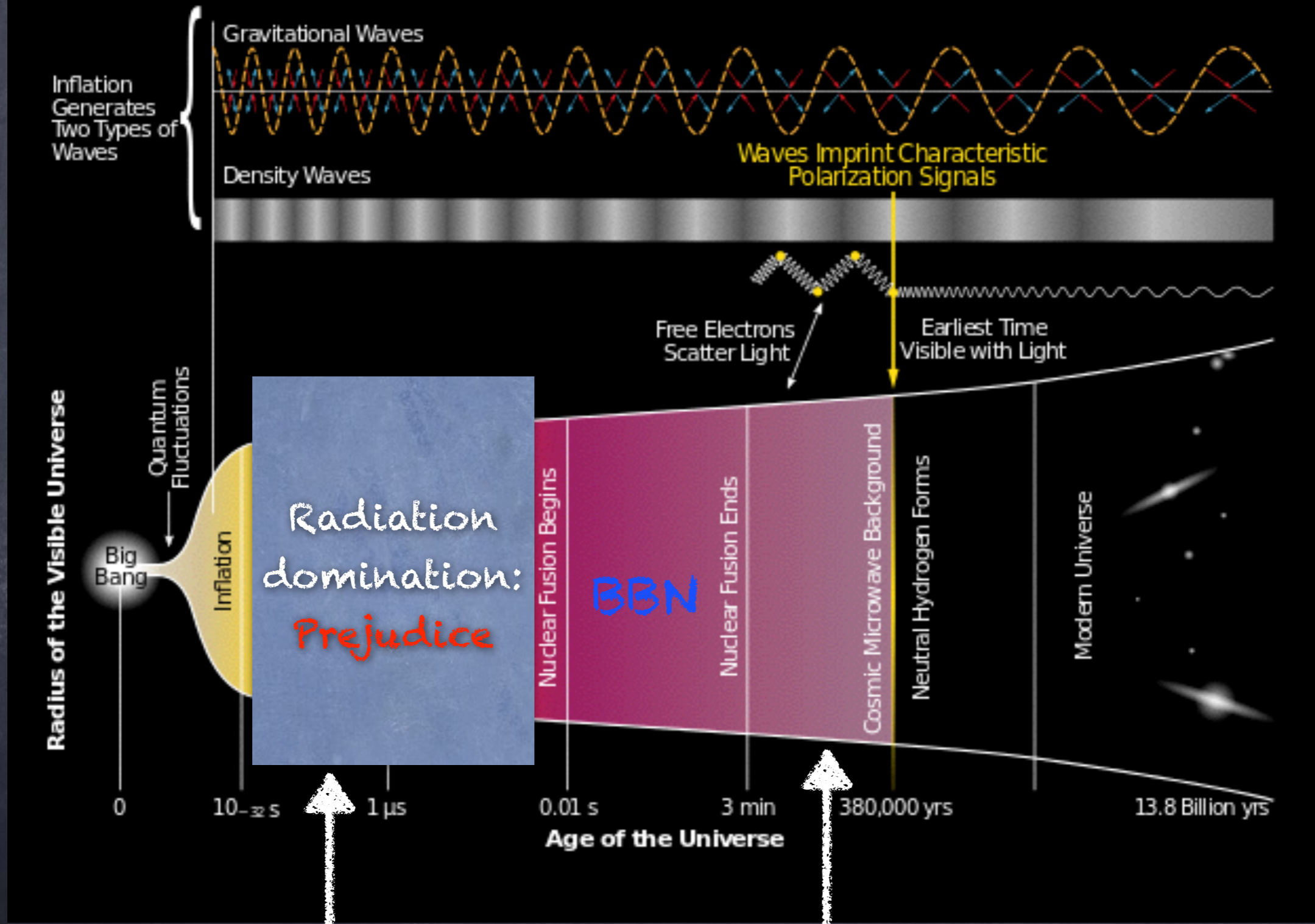
- Inflationary paradigm is the leading candidate for the early universe cosmology: Many reasons
- Must be compatible with our knowledge about high energy physics: Probably the only probe
- Consequences of precision CMB data

History of the Universe



Matter domination

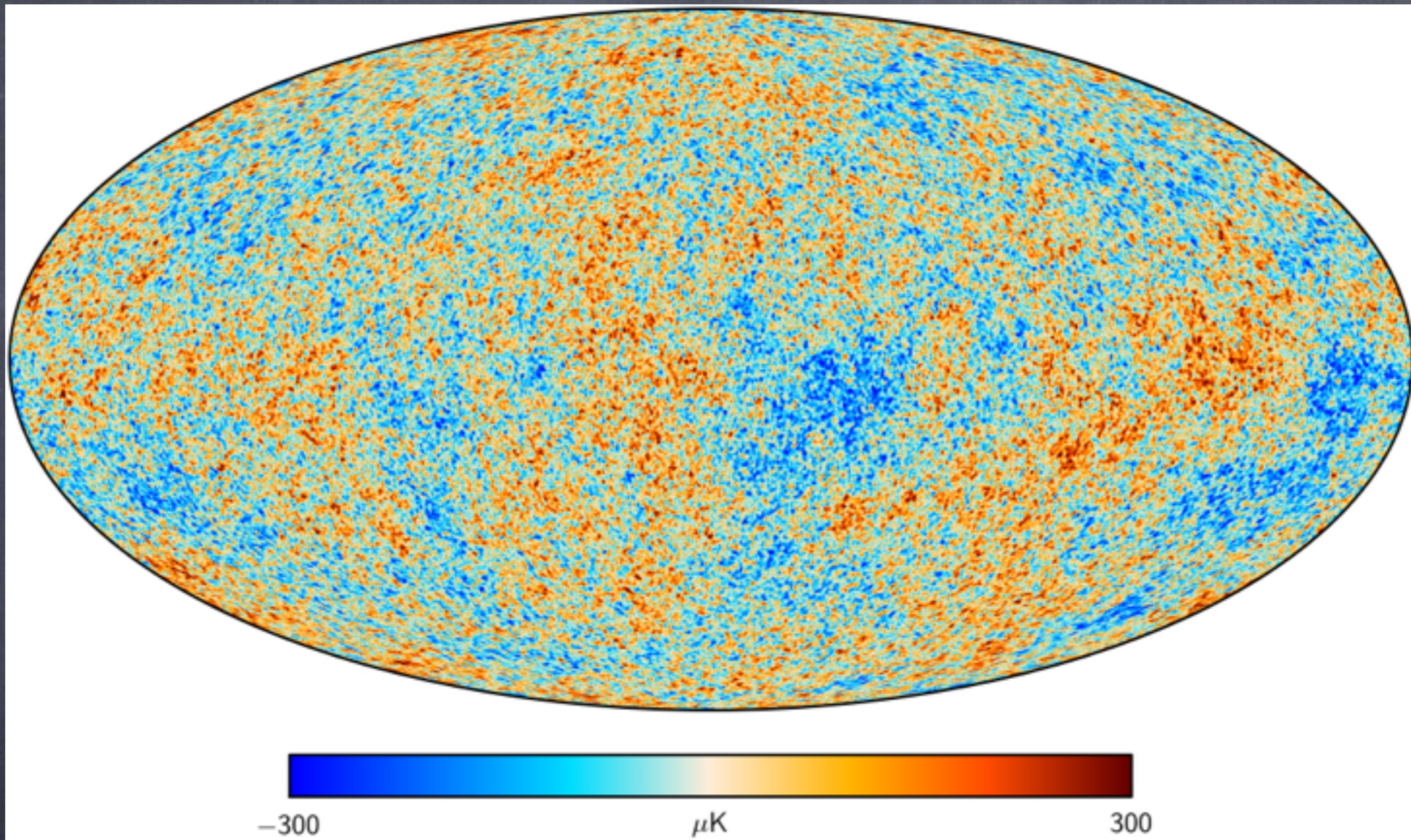
History of the Universe



non-thermal epoch

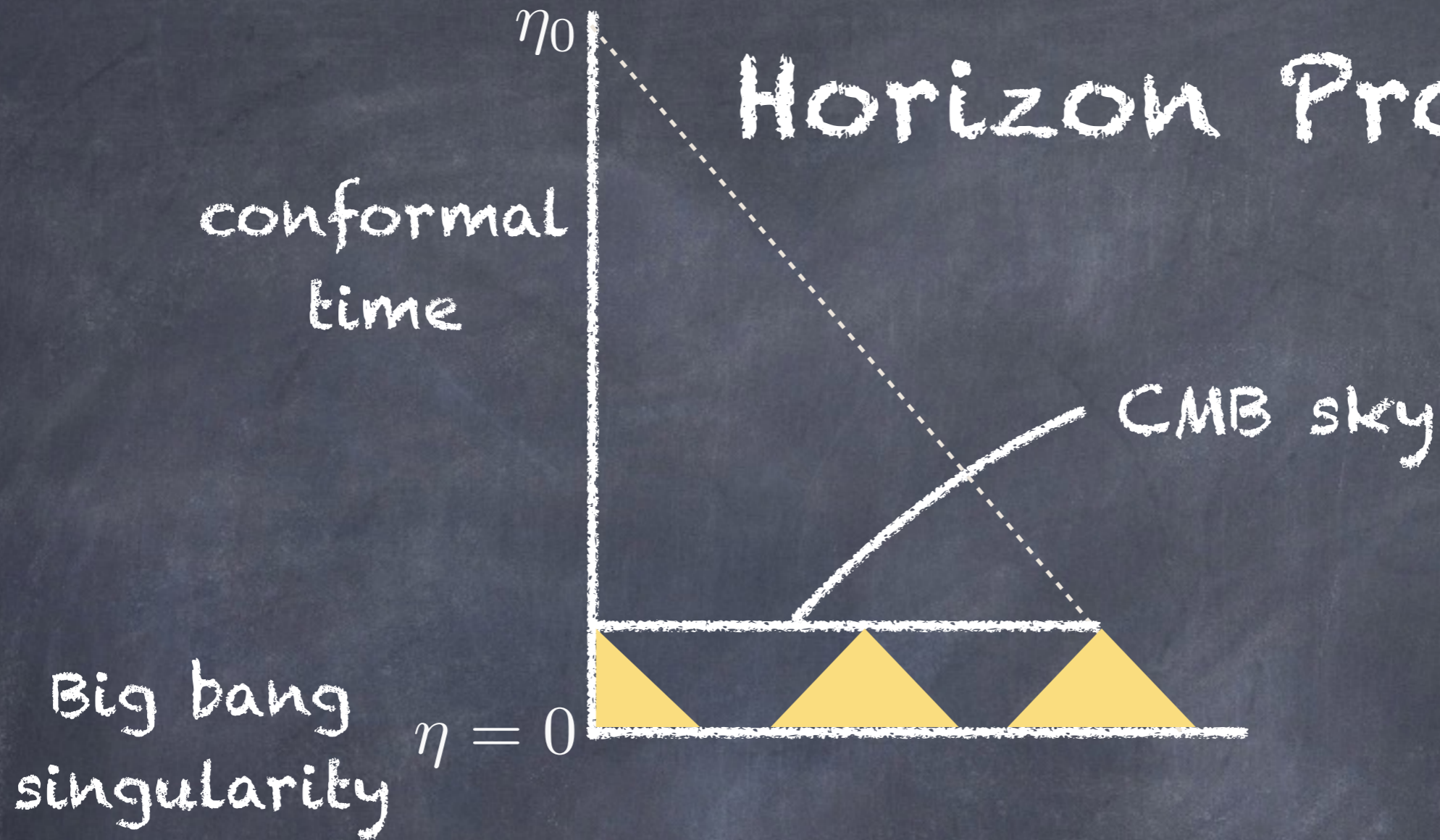
Matter domination

PLANCK 2015

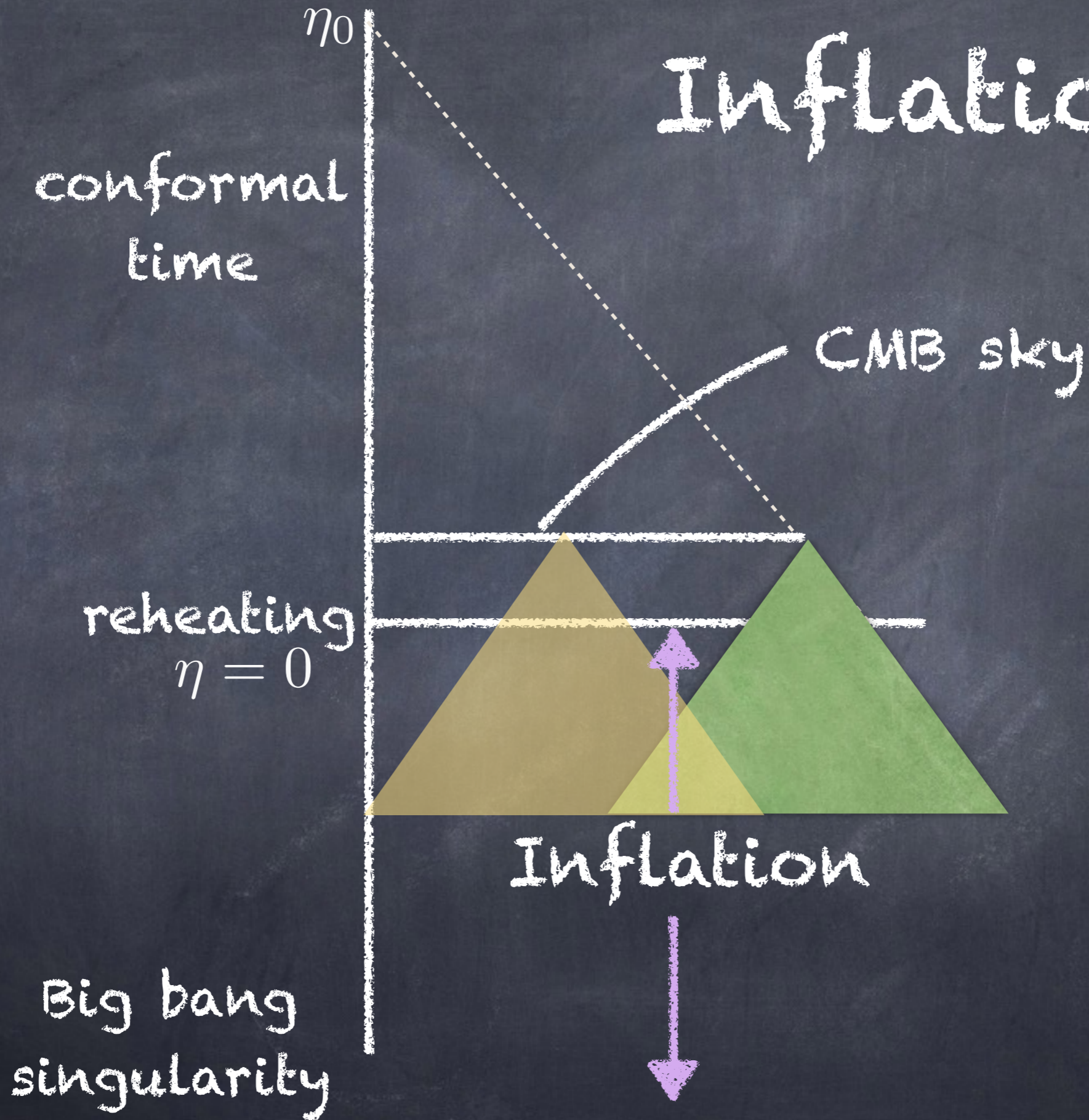


Fluctuations $\sim 0,00001$

Horizon Problem



Inflation



Inflation

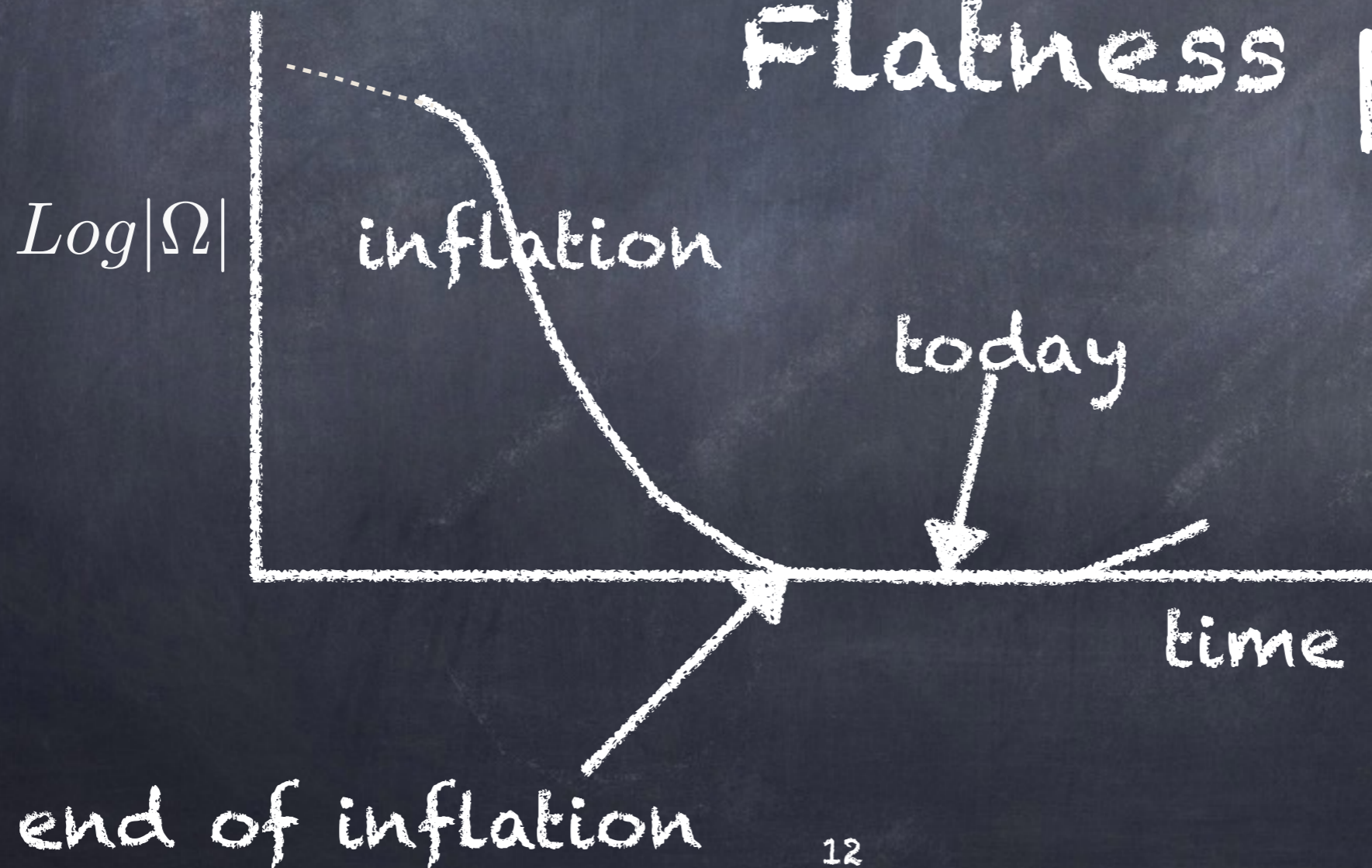
$$1 - \Omega_{Tot} = -\frac{k}{(aH)^2}$$

Flatness problem

Inflation

$$1 - \Omega_{Tot} = -\frac{k}{(aH)^2}$$

Flatness problem



Inflation

$$\frac{d}{dt}((aH)^{-1}) < 0$$

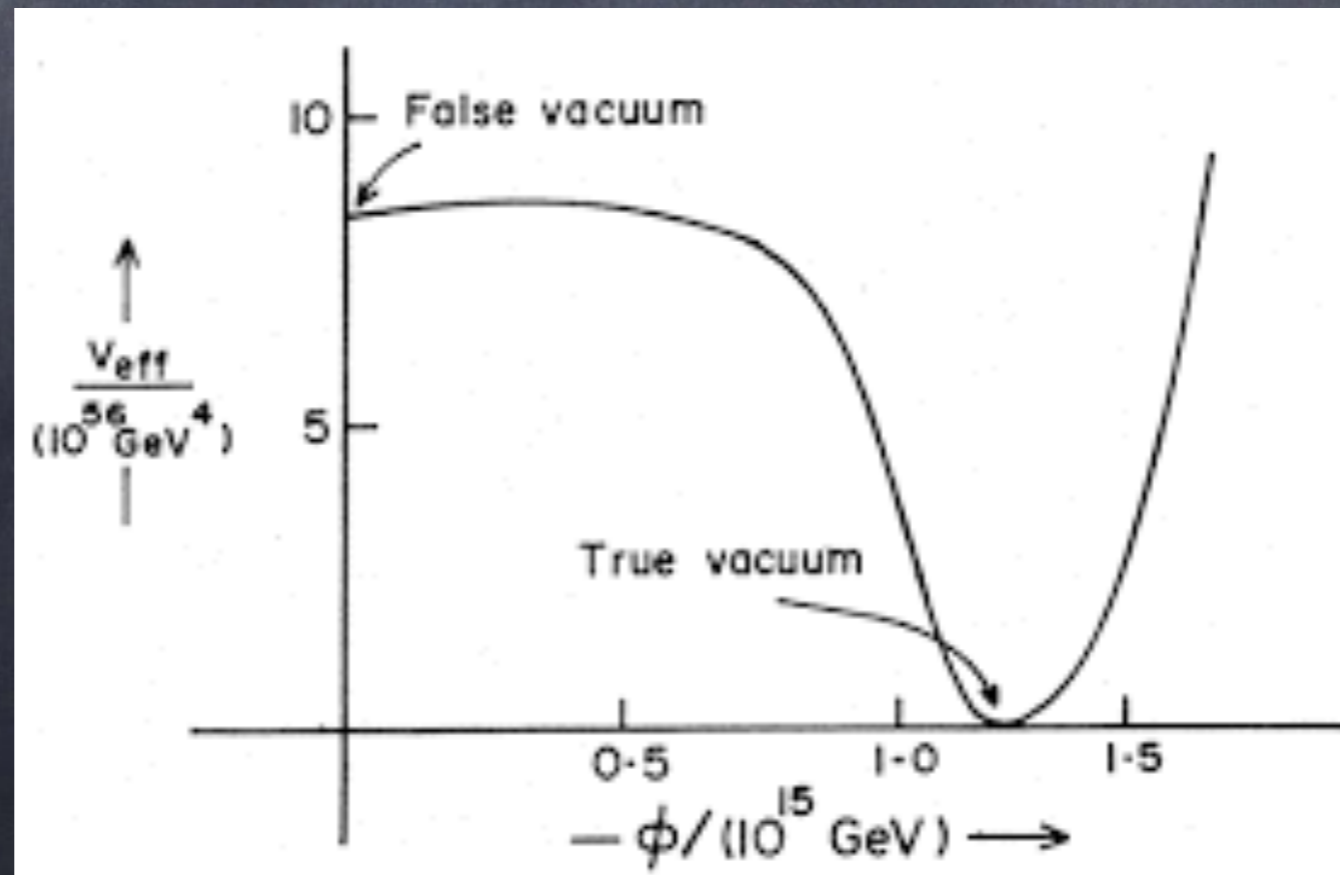


$$\ddot{a} > 0$$

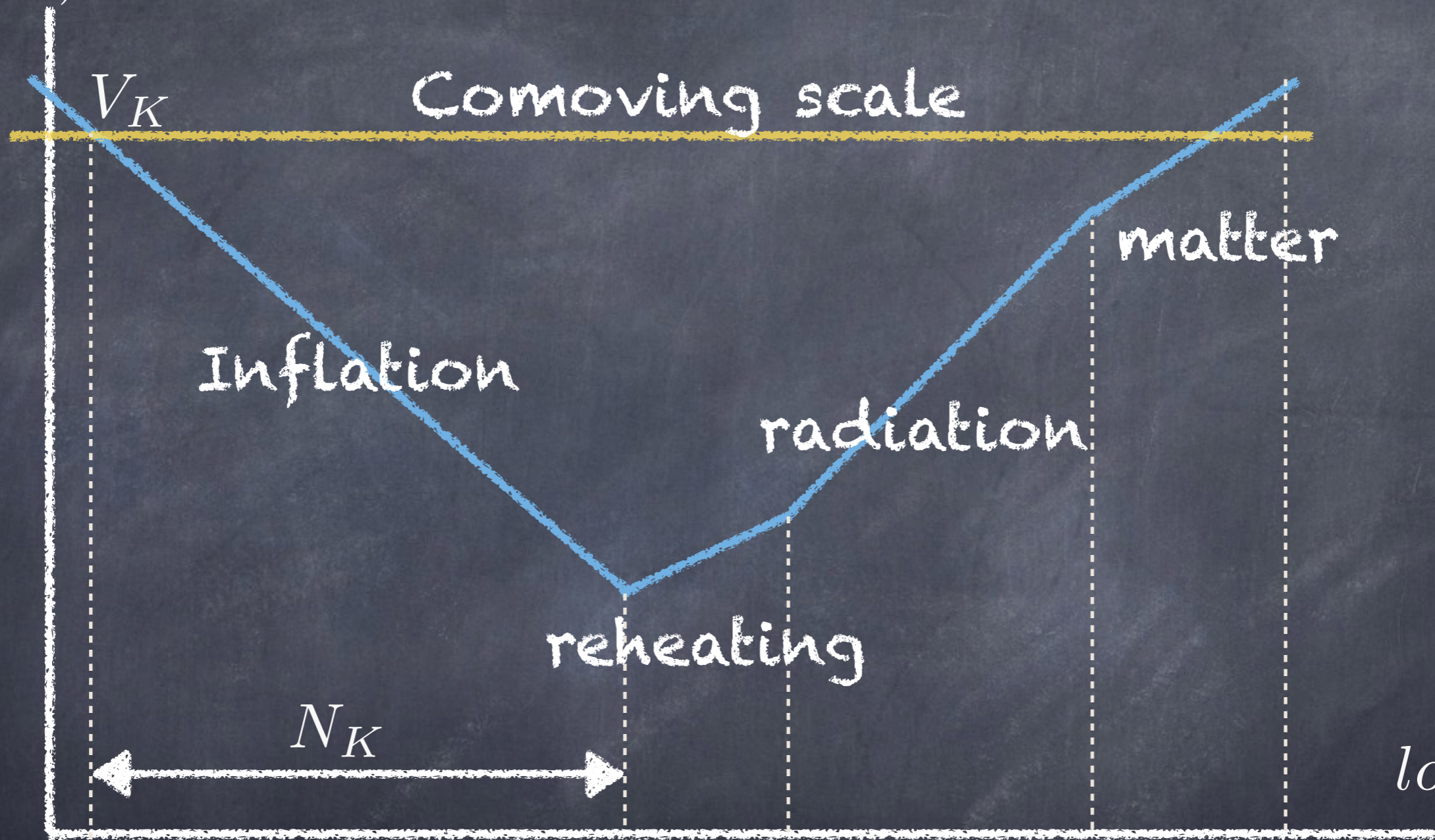
Inflation

$$\frac{d}{dt}((aH)^{-1}) < 0 \quad \longleftrightarrow \quad \ddot{a} > 0$$

implemented by 'slowly rolling' scalar field whose potential energy dominates!



$\log(1/aH)$



CMB scales
exit

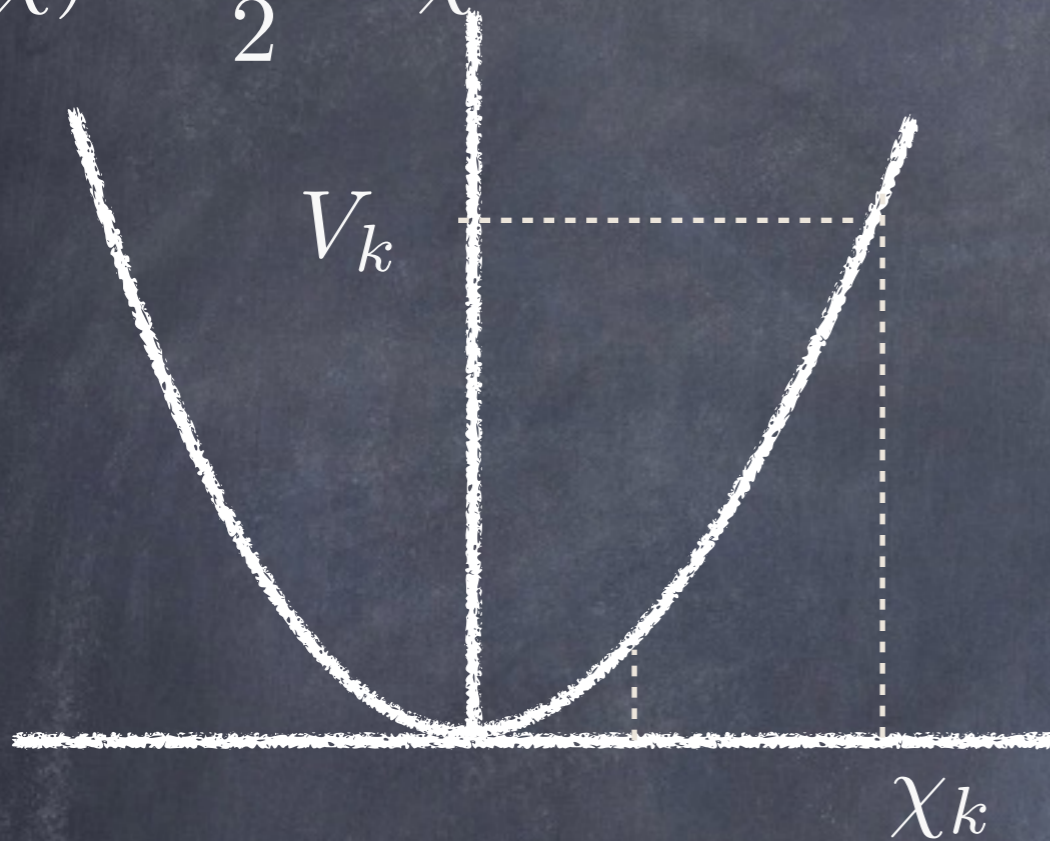
end of
inflation

today

$\log(a)$

Inflation: Case Study

$$V(\chi) = \frac{1}{2}m^2\chi^2$$

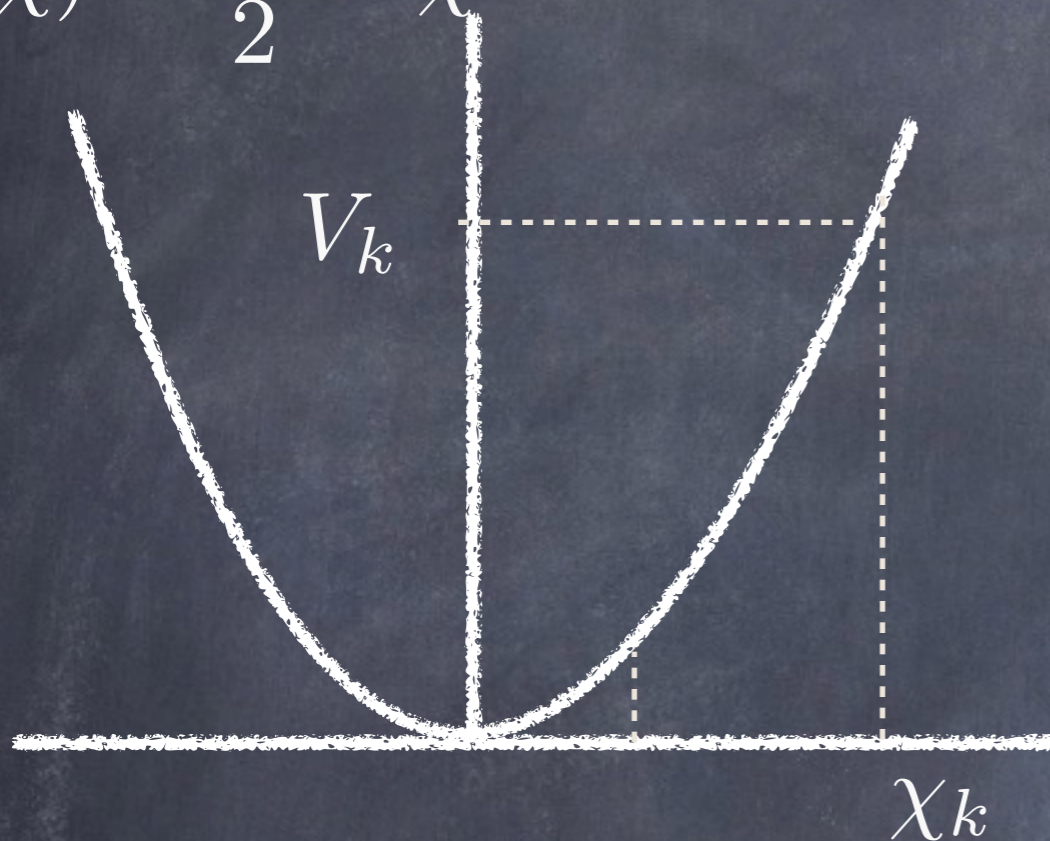


$$N_k \simeq \frac{\chi_k^2}{4M_{Pl}^2}$$

$$n_s - 1 = -\frac{2}{N_k}$$

Inflation: Case Study

$$V(\chi) = \frac{1}{2}m^2\chi^2$$



$$N_k \simeq \frac{\chi_k^2}{4M_{Pl}^2}$$

$$n_s - 1 = -\frac{2}{N_k}$$

$$n_s = 0.968 \pm 0.006$$

PLANCK 2015

precision measurement of spectral index can pin down the e-folds during inflation

Inflation & Density Perturbations

$$A_s = \frac{2}{3\pi^2 r} \left(\frac{\rho_k}{M_{Pl}^4} \right)$$

Energy density at the time
of horizon exit

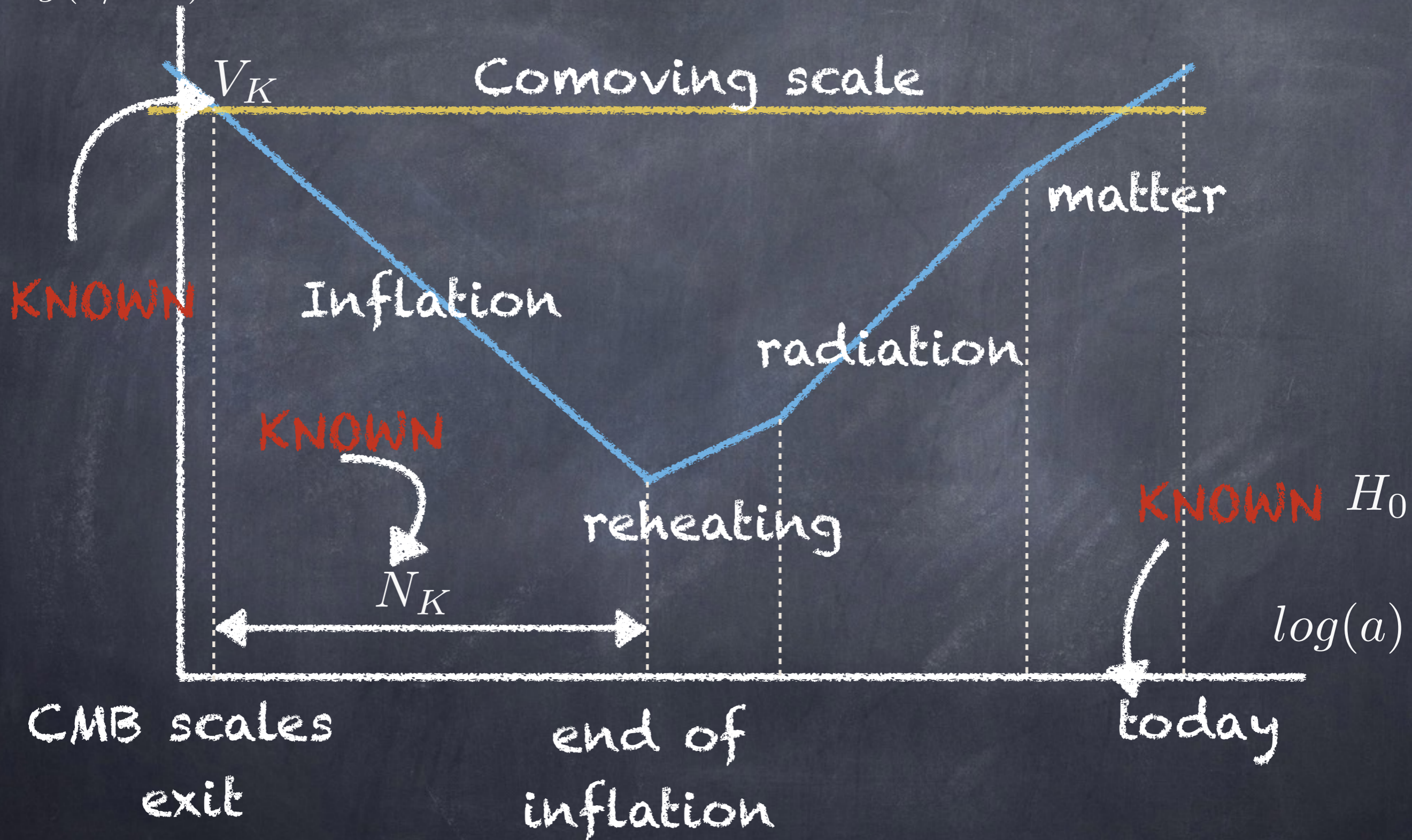
strength of gravity wave

$$A_s = 2.2 \times 10^{-9} \quad @ \quad k = 0.05 \text{Mpc}^{-1}$$

knowing scalar amplitude and 'r' we know
initial energy density

Single field inflation: A_s conserved

$\log(1/aH)$



Consistency

V_k must be evolved to H_0

Any post inflationary evolution must be evolved to the present energy density

Consistency Condition

$$N_{inf} + \frac{1}{4}(1 - 3w_{rh})N_{rh} = 55 + \frac{1}{4}\ln r + \frac{1}{4}\ln(\rho_k/\rho_{end})$$

Consistency Condition

$$N_{inf} + \frac{1}{4}(1 - 3w_{rh})N_{rh} = 55 + \frac{1}{4} \ln r + \frac{1}{4} \ln(\rho_k / \rho_{end})$$



Equivalent

$$N_* \approx 71.21 - \ln\left(\frac{k_*}{a_0 H_0}\right) + \frac{1}{4} \ln\left(\frac{V_{hor}}{M_{pl}^4}\right) + \frac{1}{4} \ln\left(\frac{V_{hor}}{\rho_{end}}\right) + \frac{1 - 3w_{int}}{12(1 + w_{int})} \ln\left(\frac{\rho_{th}}{\rho_{end}}\right),$$

PLANCK paper

Making predictions ..

$$N_{inf} + \frac{1}{4}(1 - 3w_{rh})N_{rh} = 55 + \frac{1}{4}\ln r + \frac{1}{4}\ln(\rho_k/\rho_{end})$$

$$N_{inf} = 55 \pm 5$$

Making predictions ..

$$N_{inf} + \frac{1}{4}(1 - 3w_{rh})N_{rh} = 55 + \frac{1}{4}\ln r + \frac{1}{4}\ln(\rho_k/\rho_{end})$$

$$N_{inf} = 55 \pm 5$$

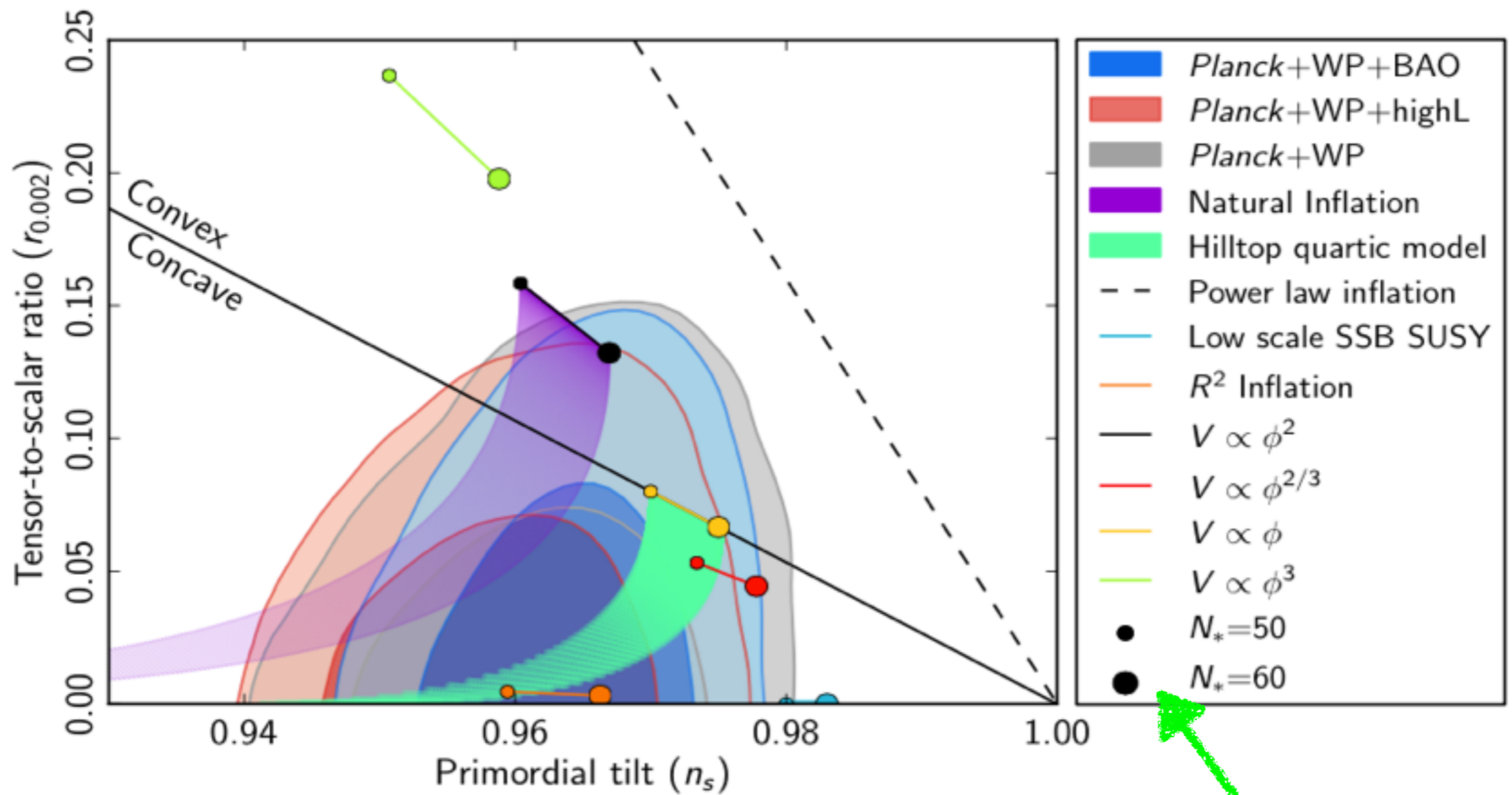
'Theoretical prior'

compute observables in terms of N_{inf} and see whether it fits data for $N = 50-60$!

$$V(\chi) = \frac{1}{2}m^2\chi^2$$

$$n_s - 1 = -\frac{2}{N_k}$$

$$r = 8/N_K$$



'Theoretical prior'

How does making
predictions change for
modular cosmology?

Moduli ..

- moduli: light scalar fields with Planck suppressed interactions
- at tree level effective Lagrangian of string theory/SUGRA, moduli are massless
- moduli must acquire masses (thus fixed vev) to become phenomenologically viable
- moduli stabilisation: KKLT etc....

Moduli ..

- Conservative approach: Make ALL modulus much heavier than the Hubble scale ..
decouple from inflation
- Wishful
- In practice, few fields remain parametrically light in the post-inflationary vacua .. (e.g Many LVS constructions ..)

A typical case

$$\mathcal{L} \supset -\frac{1}{2}m^2\varphi^2 - \frac{1}{2}H^2(\varphi - \hat{\varphi})^2 - V_{inf}(\chi)$$

$$m < H_{inf}$$

↑
post-inflationary
moduli mass

↑
minima during
inflation

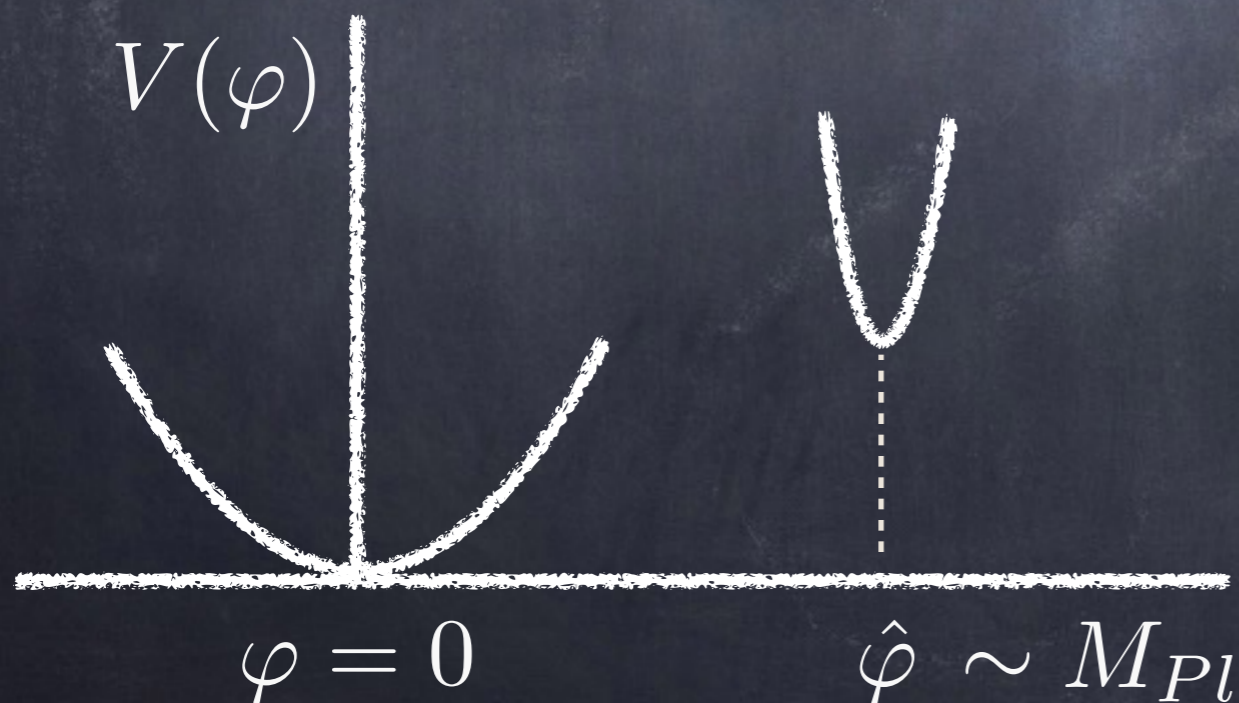
A typical case

$$\mathcal{L} \supset -\frac{1}{2}m^2\varphi^2 - \frac{1}{2}H^2(\varphi - \hat{\varphi})^2 - V_{inf}(\chi)$$

$$m < H_{inf}$$

↑
post-inflationary
moduli mass

↑
minima during
inflation



$$Y = \hat{\varphi}/M_{Pl} \sim 1$$

Dine, Randall, Thomas (1995)

SUGRA ...

$$V = e^{K[\varphi, \bar{\varphi}]} V_0[\varphi, \chi] \sim H^2 M_{Pl}^2 f \left(\frac{\varphi}{M_{Pl}} \right)$$

$$V'' \sim H^2$$

η - problem

Scale of variations M_{Pl}

$$Y = \hat{\varphi} / M_{Pl} \sim 1$$

Dine, Randall, Thomas (1995)

Dvali (1995)

SUGRA ...

$$V = e^{K[\varphi, \bar{\varphi}]} V_0[\varphi, \chi] \sim H^2 M_{Pl}^2 f \left(\frac{\varphi}{M_{Pl}} \right)$$

$$V'' \sim H^2$$

η - problem

Scale of variations M_{Pl}

$$Y = \hat{\varphi} / M_{Pl} \sim 1$$

Dine, Randall, Thomas (1995)

Dvali (1995)

Toy example ..

$$V = (m_{3/2}^2 - a^2 H^2) |\varphi|^2 + \frac{1}{2M_{Pl}^2} (m_{3/2}^2 + b^2 H^2) |\varphi|^4$$

$$\hat{\varphi} \sim (a/b) M_{Pl}$$

"Fibre inflation" ..

Cicoli, Burgess, Quevedo

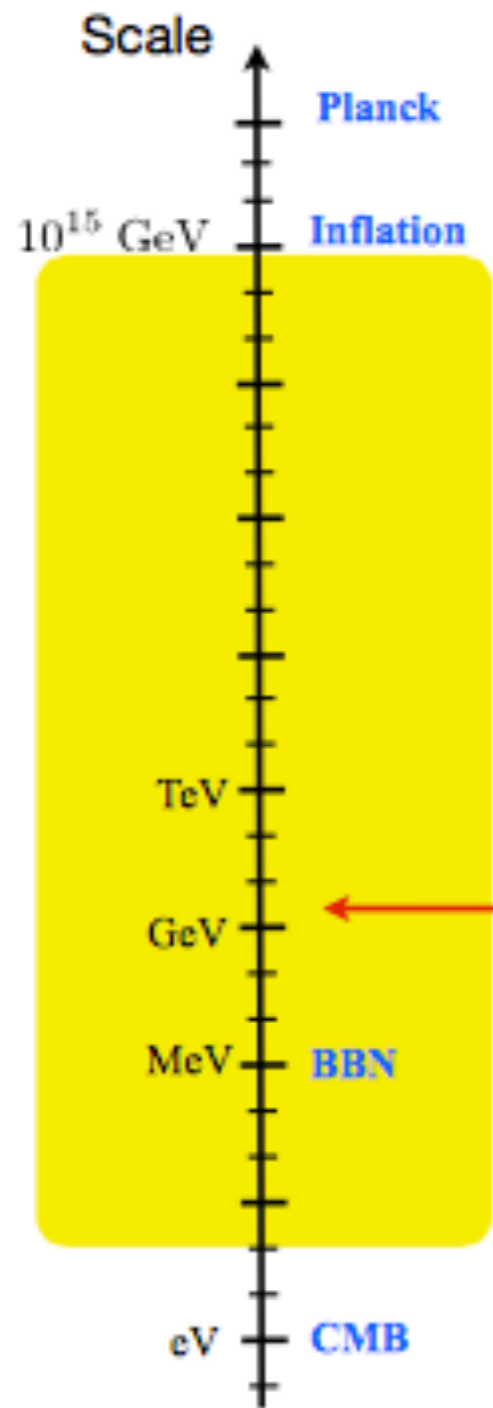
$$\hat{\varphi} \sim 0.1 M_{Pl}$$

Sequence of events ..

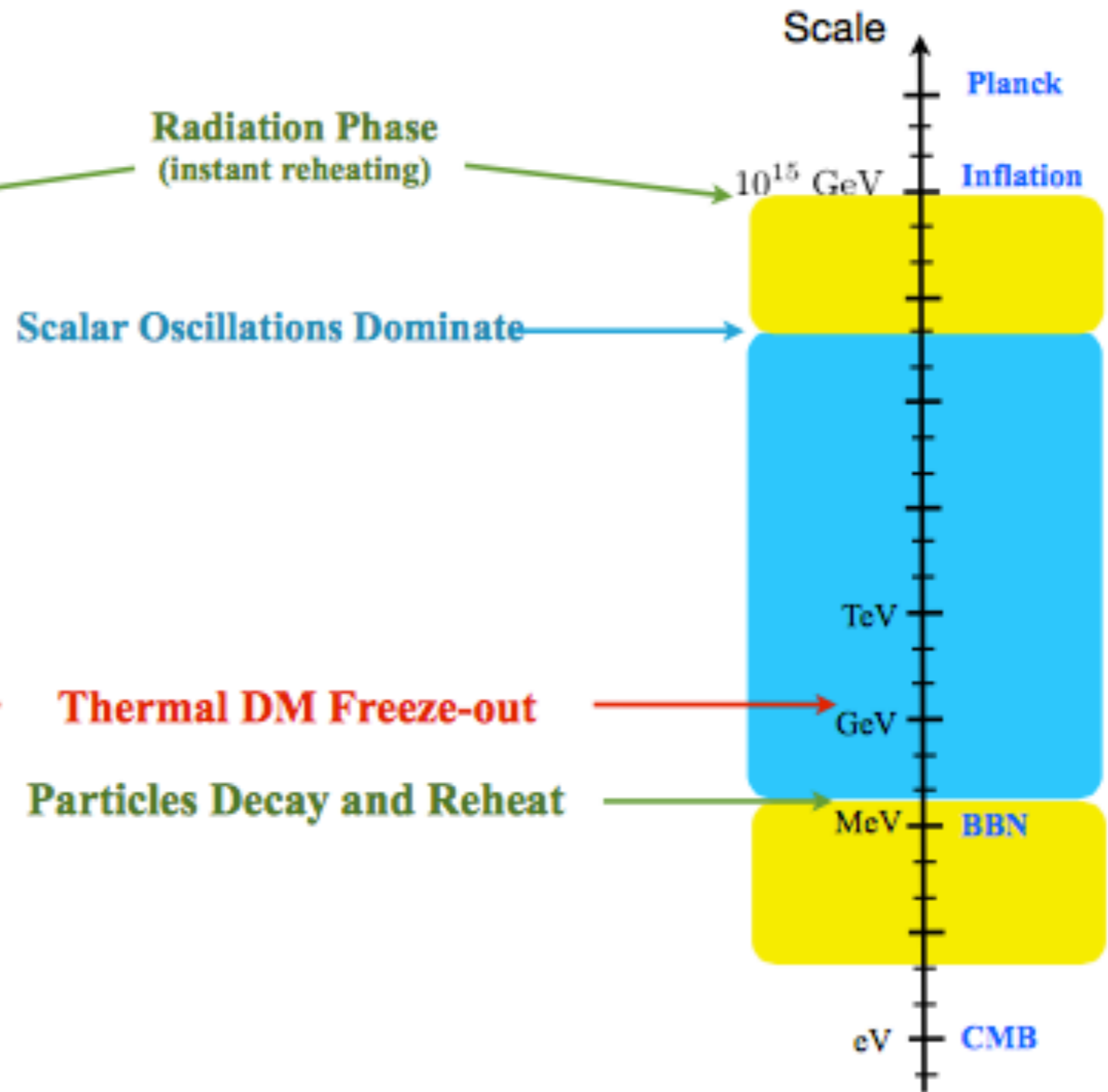
- when $m < H_{\text{inf}}$, moduli is stuck due to the Hubble friction
- inflation ends with $\varphi = \hat{\varphi}$
- When $H < m$, the field starts to move toward its post inflationary minima $\varphi = 0$
- Oscillations around the minima behaves as matter $\rho_{\varphi} \sim a^{-3}(t)$

Review: B. S. Acharya,
G. Kane, and P. Kumar
(2012)

Thermal History



Alternative History



Kane, Sinha, Watson
(2015)

Consistency

V_k must be evolved to H_0

N_k is known

Any post inflationary evolution must be evolved to the present energy density

Decay of Modulus

moduli must decay so that it does not
overclose the Universe

$$\Gamma_{mod} \sim \frac{m_{\varphi}^3}{16\pi M_{Pl}^2}$$

G. D. Coughlan, W.
Fischler, E. W. Kolb, S.
Raby and G. G. Ross 1984

Decay of Modulus

moduli must decay so that it does not overclose the Universe

$$\Gamma_{mod} \sim \frac{m_\phi^3}{16\pi M_{Pl}^2}$$

G. D. Coughlan, W. Fischler, E. W. Kolb, S. Raby and G. G. Ross 1984

$$\rho_{mod}(t_{decay}) = g \frac{\pi^2}{30} T_{reheat}^4 = 3H^2 M_{Pl}^2$$

↑ decay happens
 Γ_{mod}

Decay of Modulus

moduli must decay so that it does not overclose the Universe

$$\Gamma_{mod} \sim \frac{m_\phi^3}{16\pi M_{Pl}^2}$$

G. D. Coughlan, W. Fischler, E. W. Kolb, S. Raby and G. G. Ross 1984

$$\rho_{mod}(t_{decay}) = g \frac{\pi^2}{30} T_{reheat}^4 = 3H^2 M_{Pl}^2$$

↑ decay happens
 Γ_{mod}

$$T_{reheat} \sim \sqrt{\Gamma M_{Pl}} \quad T_{reheat} > MeV \quad \text{successful BBN}$$

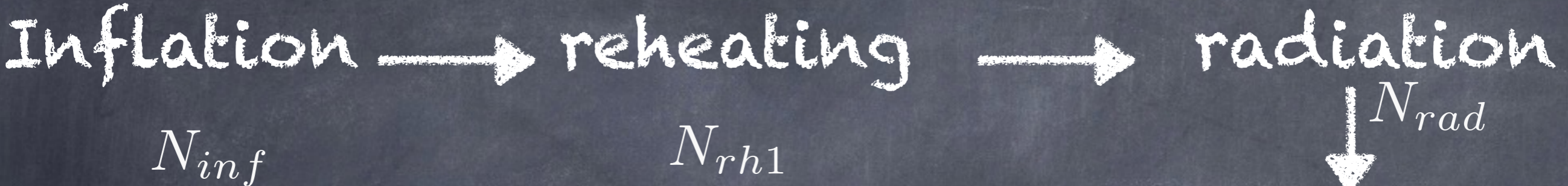
$$m_\phi > 30 TeV \quad \text{BBN bound}$$

phenomenological implications .. SUSY

Inflation \longrightarrow reheating \longrightarrow radiation
 N_{inf} N_{rh1} N_{rad}

reheating \longleftarrow moduli (matter)
 N_{rh2} 'non-standard' N_{mod}

BBN
 \downarrow
today



K.D, Maharana

arXiv:1409.7037[hep-ph]

$$N_{inf} + \frac{1}{4}(1 - 3w_{rh1})N_{rh1} + \frac{1}{4}N_{mod} + \frac{1}{4}(1 - 3w_{rh2})N_{rh2}$$

$$= 55.43 + \frac{1}{4} \ln r + \frac{1}{4} \ln \left(\frac{\rho_k}{\rho_{end}} \right)$$

non-thermal history

constraint ..

$$\Gamma_{mod} \sim \frac{m_\phi^3}{16\pi M_{Pl}^2}$$

$$N_{mod} \sim \frac{2}{3} \ln\left(\frac{16\pi M_{Pl}^2 Y^4}{m_\phi^2}\right)$$

initial displacement $Y = \hat{\phi}/M_{Pl}$

constraint ..

$$\Gamma_{mod} \sim \frac{m_\phi^3}{16\pi M_{Pl}^2} \quad N_{mod} \sim \frac{2}{3} \ln\left(\frac{16\pi M_{Pl}^2 Y^4}{m_\phi^2}\right)$$

initial displacement $Y = \hat{\phi}/M_{Pl}$

$$\frac{1}{6} \ln\left(\frac{16\pi M_{Pl}^2 Y^4}{m_\phi^2}\right) + \frac{1}{4}(1 - 3w_{rh1})N_{re1} + \frac{1}{4}(1 - 3w_{rh2})N_{re2}$$

$$= 55.43 - N_{inf} + \frac{1}{4} \ln r + \frac{1}{4} \ln\left(\frac{\rho_k}{\rho_{end}}\right)$$

analytical/numerical
understanding of
reheating: $w_{re} < 1/3$

inflationary
potentials

$$\begin{aligned}
& N_{inf} + \frac{1}{4}(1 - 3w_{rh1})N_{rh1} + \frac{1}{4}(1 - 3w_{rh2})N_{rh2} \\
& = 55 - \frac{1}{3} \left(\frac{\sqrt{16\pi} M_{Pl} Y^2}{m_\varphi} \right) + \frac{1}{4} \ln r + \frac{1}{4} \ln \left(\frac{\rho_k}{\rho_{end}} \right)
\end{aligned}$$

- central value shifts

- significant impact for inflation models

Implications: I

Central value of e-folding shifts

$$N_{inf} = 55 \pm 5$$



$$N_{inf} = \left(55 - \frac{N_{mod}}{4} \right) \pm 5$$

$$N_{inf} = \left(55 - \frac{1}{3} \ln \left(\frac{\sqrt{16\pi} M_{pl} Y^2}{m_\varphi} \right) \right) \pm 5 \quad \Gamma_{mod} \sim \frac{m_\varphi^3}{16\pi M_{Pl}^2}$$

$$N_{inf} = \left(55 - \frac{1}{3} \ln \left(\frac{\sqrt{16\pi} M_{pl} Y^2}{m_\varphi} \right) \right) \pm 5$$

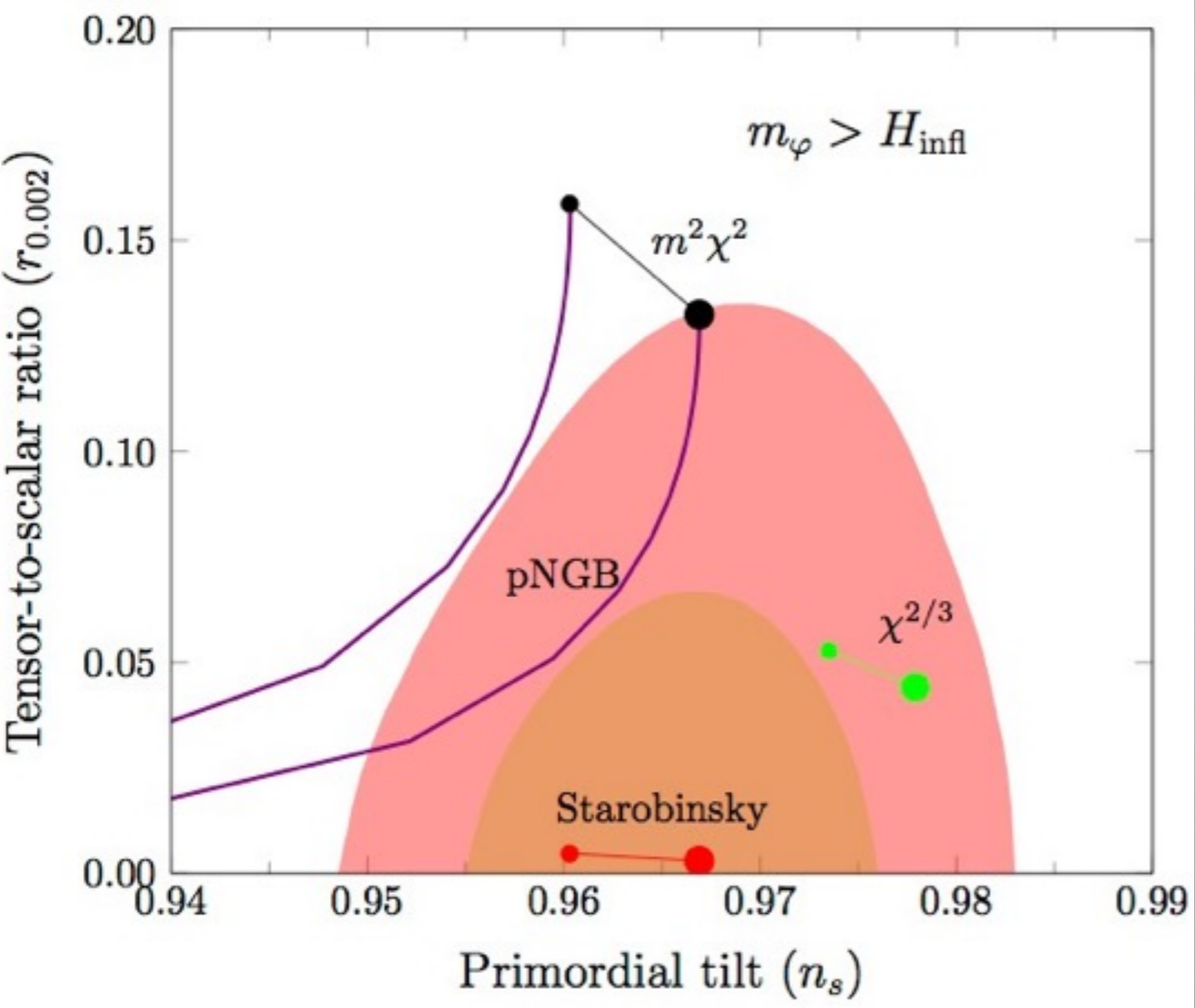
Central value of e folding shifts

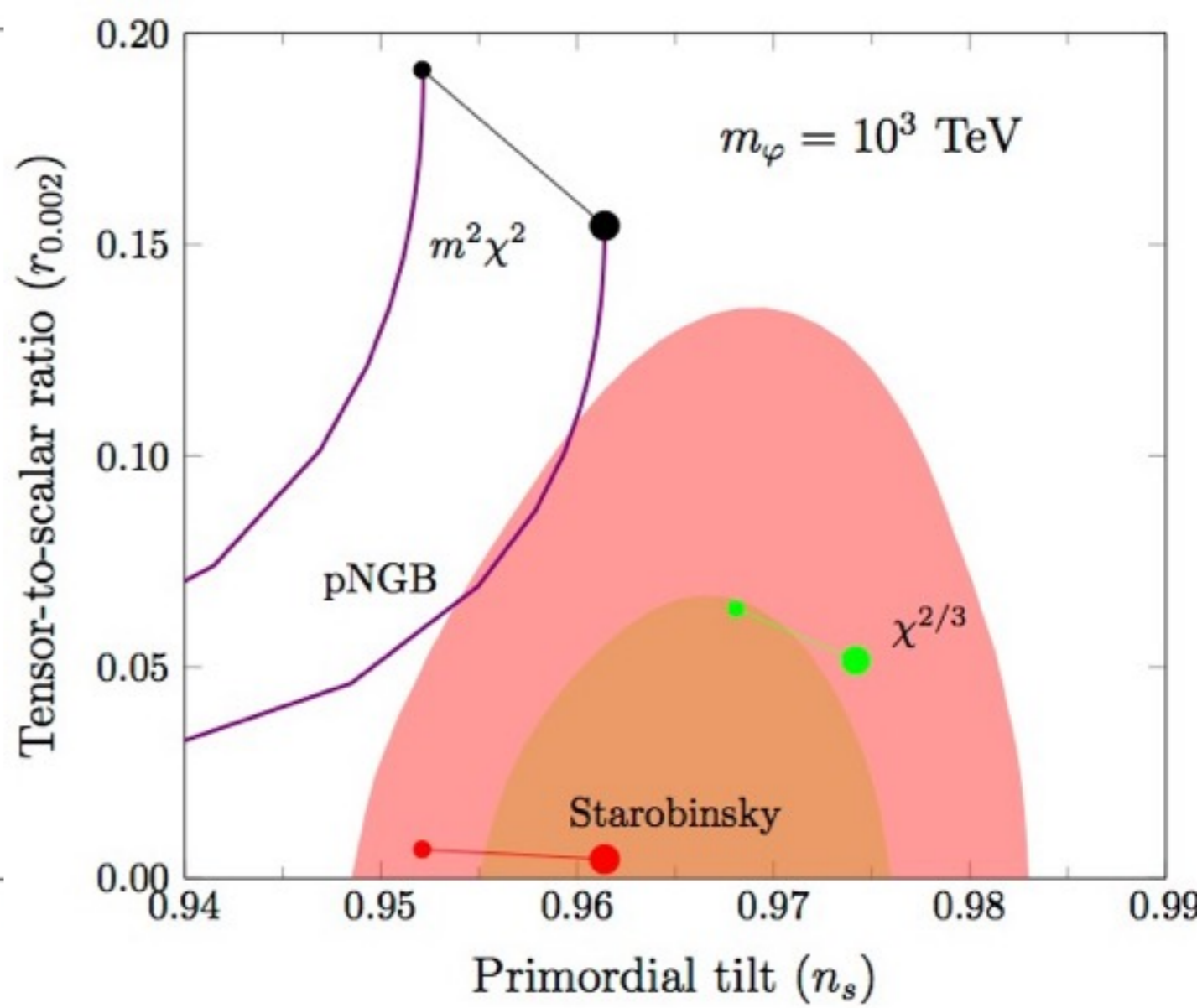
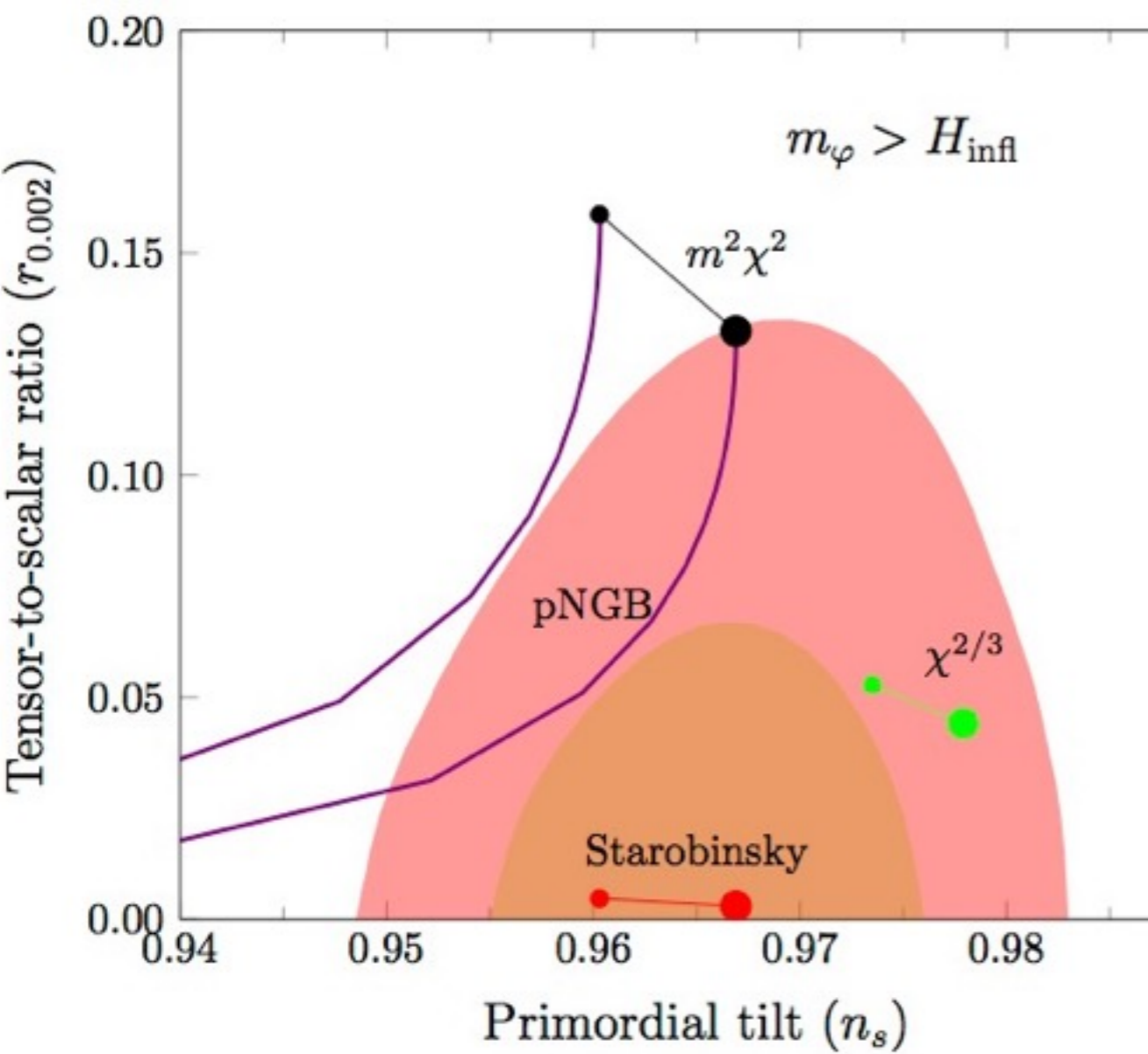
For $m_\varphi \sim 10^3$ TeV : $N_{inf} = 41 - 51$

For $m_\varphi \sim 10^6$ TeV : $N_{inf} = 43 - 53$

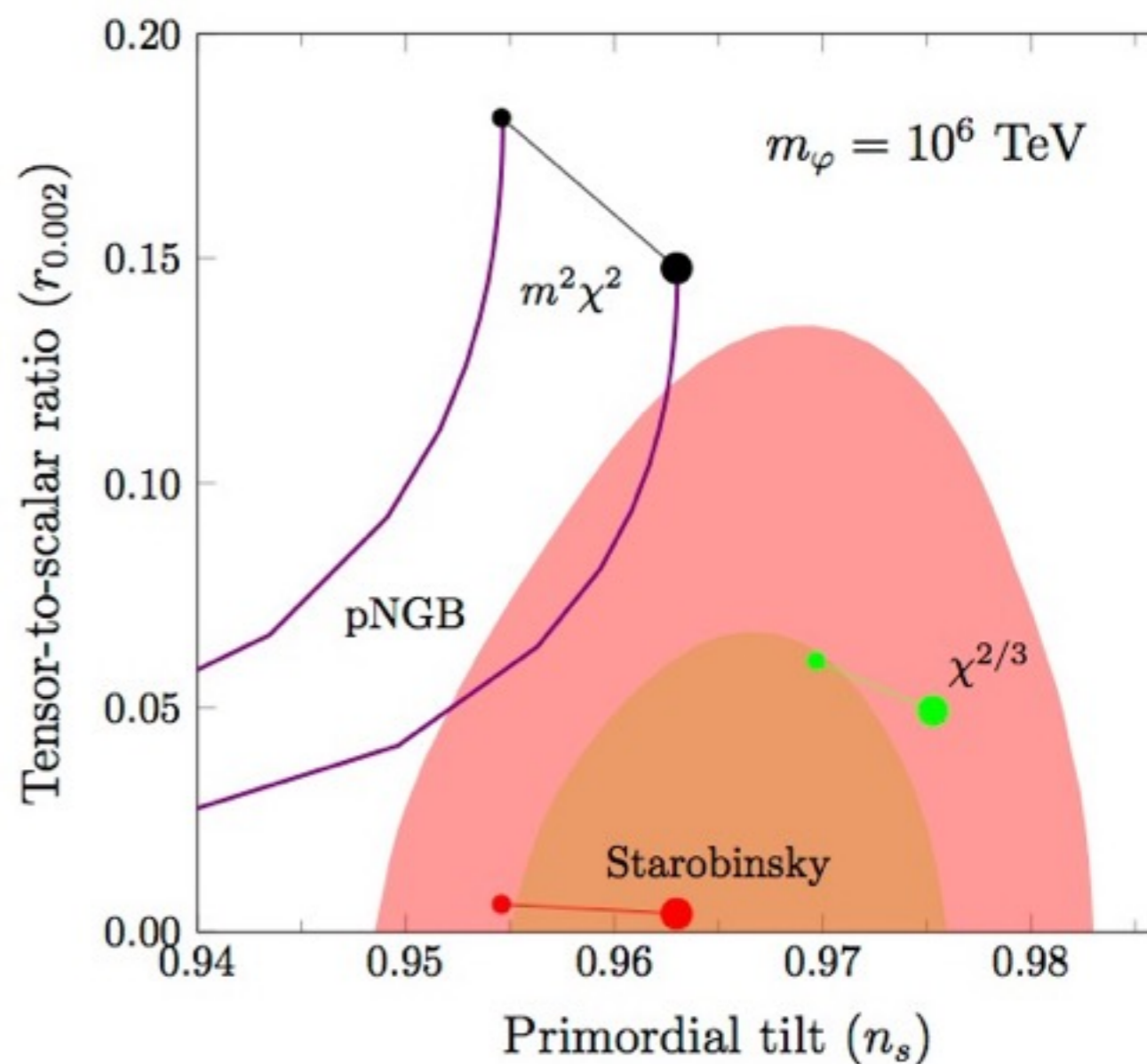
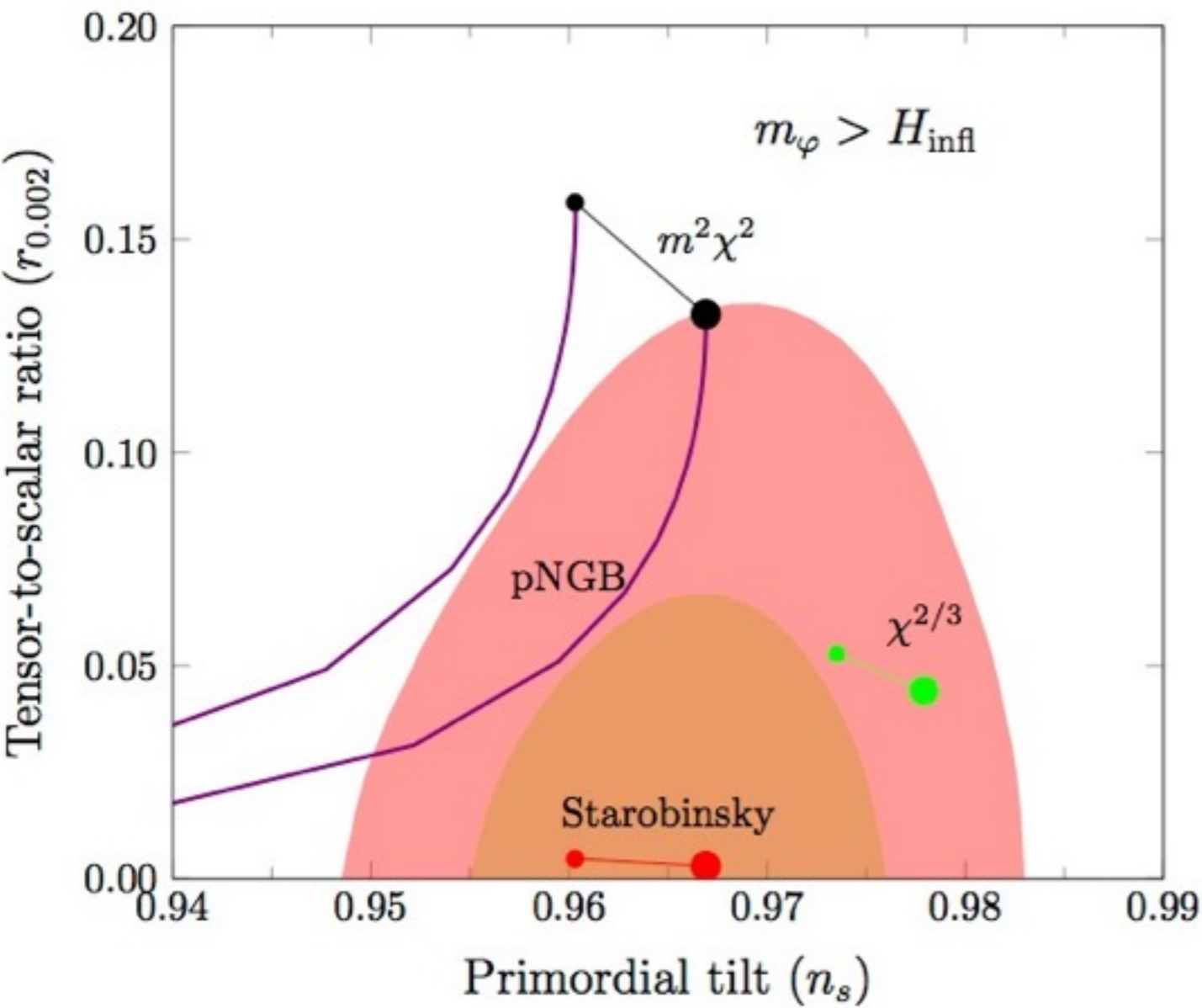
(used to be 50 - 60)

($Y \sim 0.1$ assumed)





Das, Maharana, K.D



Das, Maharana, K.D

sensitivity $n_s \sim 10^{-3}$

DECIGO/PRISM/21 Cm

The central value reaches $N = 50$ for

$$m_\varphi \sim 10^{10} \text{ GeV}$$

The effects of modulus mass must be taken for inflation models for $m_\varphi \lesssim 10^{10} \text{ GeV}$

constraint on modulus mass

$$\frac{1}{6} \ln\left(\frac{16\pi M_{Pl}^2 Y^4}{m_\varphi^2}\right) + \frac{1}{4}(1 - 3w_{rh1})N_{re1} + \frac{1}{4}(1 - 3w_{rh2})N_{re2}$$

usually positive definite

$$= 55.43 - N_{inf} + \frac{1}{4} \ln r + \frac{1}{4} \ln\left(\frac{\rho_k}{\rho_{end}}\right)$$

analytical/numerical
understanding of
reheating: $w_{re} < 1/3$

Ellis, Garcia, Nanopoulos, Olive

1505.06986

constraint ..

$$m_\varphi \gtrsim \sqrt{16\pi} M_{\text{pl}} Y^2 e^{-3\left(55.43 - N_k + \frac{1}{4} \ln\left(\frac{\rho_k}{\rho_{\text{end}}}\right) + \frac{1}{4} \ln r\right)}$$

- Dependence correlated
- larger the value of N_{inf} , stronger the bound
- smaller the value of 'r' stronger the bound
- bound depends on the nature of inflationary potentials via the ratio of energy densities

small field models

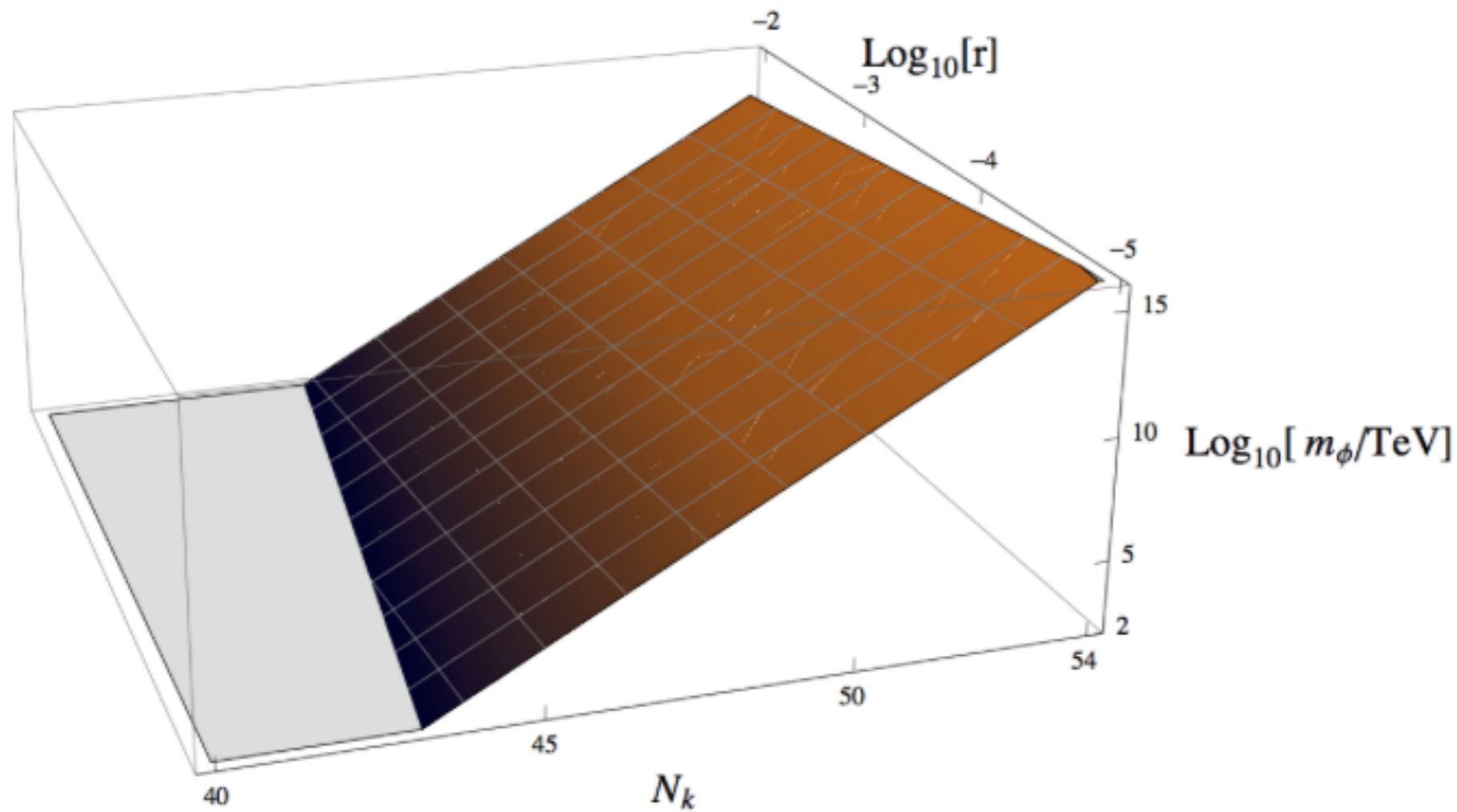
$$m_\varphi \gtrsim \sqrt{16\pi} M_{\text{pl}} Y^2 e^{-3\left(55.43 - N_k + \frac{1}{4} \ln\left(\frac{\rho_k}{\rho_{\text{end}}}\right) + \frac{1}{4} \ln r\right)}$$

- conservative estimate $r \sim 0.01$ stronger the bound
- potential plateau like .. ratio of energy densities negligible
- take $Y = 0.01$, then for $N = 50$

$$m_\varphi \gtrsim 4.5 \times 10^6 \text{ TeV}$$

much stronger than BBN bound

small field models



for $N > 44.5$,
the bound
much
stronger than
BBN bound

Fibre Inflation: $r < 0.01$ and $N > 50$ for CMB
observations

Large field models

$$m_\varphi \gtrsim \sqrt{16\pi} M_{\text{pl}} Y^2 e^{-3 \left(55.43 - N_k + \frac{1}{4} \ln \left(\frac{\rho_k}{\rho_{\text{end}}} \right) + \frac{1}{4} \ln r \right)}$$

$$V_\chi = m^{4-\alpha} \chi^\alpha$$

chaotic inflation
axion monodromy

$$m_\phi \gtrsim$$

$$\sqrt{16\pi} M_{\text{pl}} Y^2 e^{-3 \left(55.85 - \frac{(2+\alpha)}{2(1-n_s)} + \frac{\alpha}{8} \ln 2 + \frac{1}{8} (\alpha-2) \ln \left(\frac{2+\alpha}{\alpha(1-n_s)} \right) \right)}$$

$\alpha = 2$, $m_\varphi \gg H_{\text{inf}}$ Modular cosmology incompatible

$m_\varphi \gg 10^{10}$ TeV PLANCK: 1-sigma lower limit

$\alpha = 2/3$ Bound insignificant

Implications

- guiding principle for modular cosmology
(Independent from CMP bound)
- modulus mass related to soft masses in SUSY
(gravity mediated SUSY breaking)
- Large SUSY breaking scale ...
- for many models $N_k > 50$, and the bound is much stronger than BBN bound for PLANCK central value ..

Conclusions

- modulus dominated cosmology is a generic feature of string/sugra motivated scenario

Conclusions

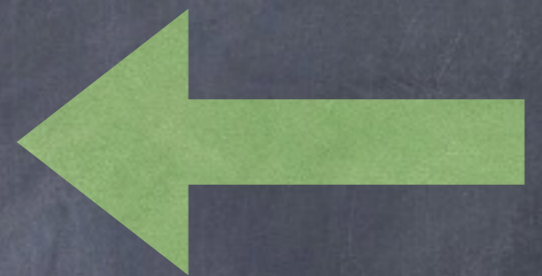
- modulus dominated cosmology is a generic feature of string/sugra motivated scenario

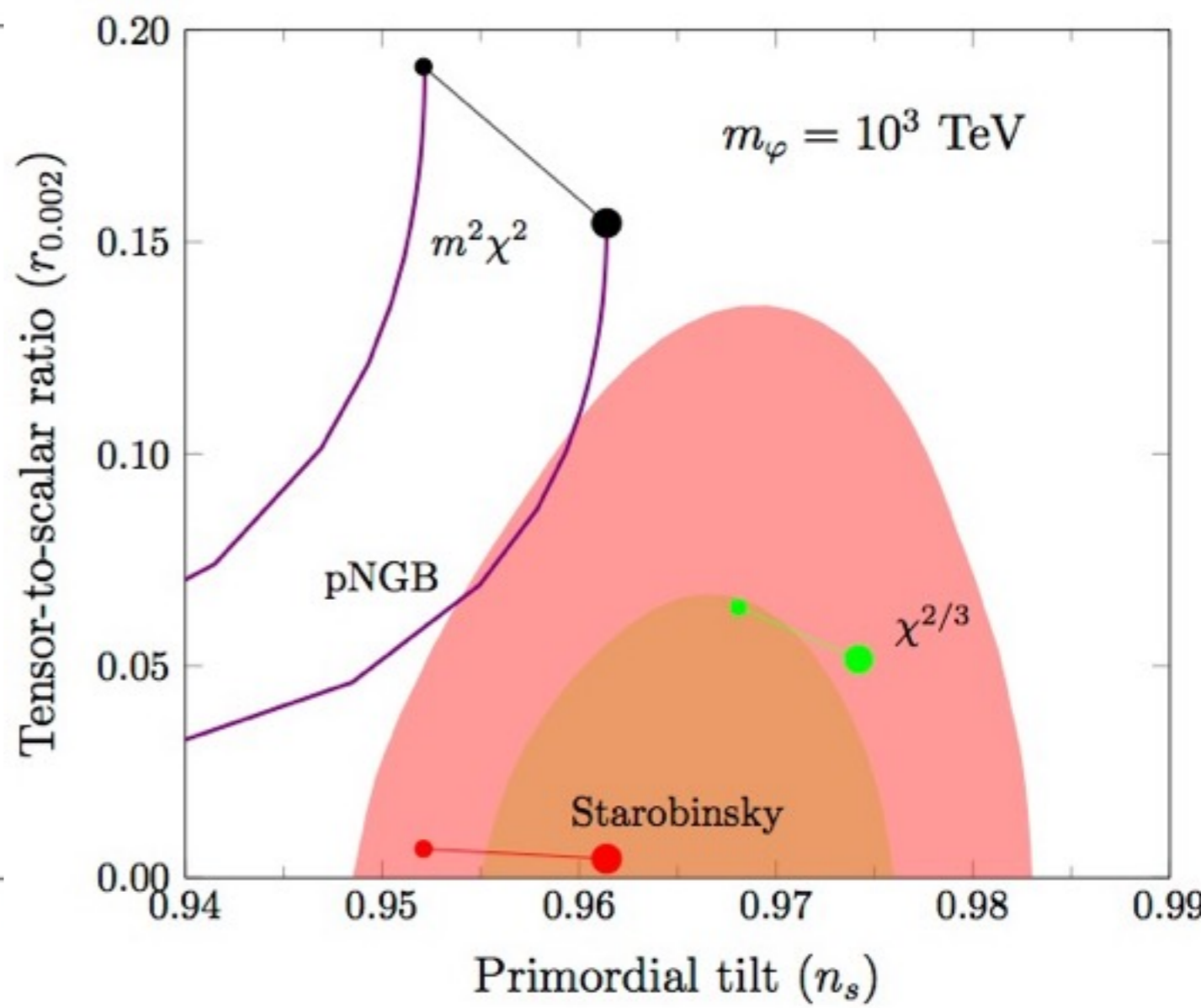
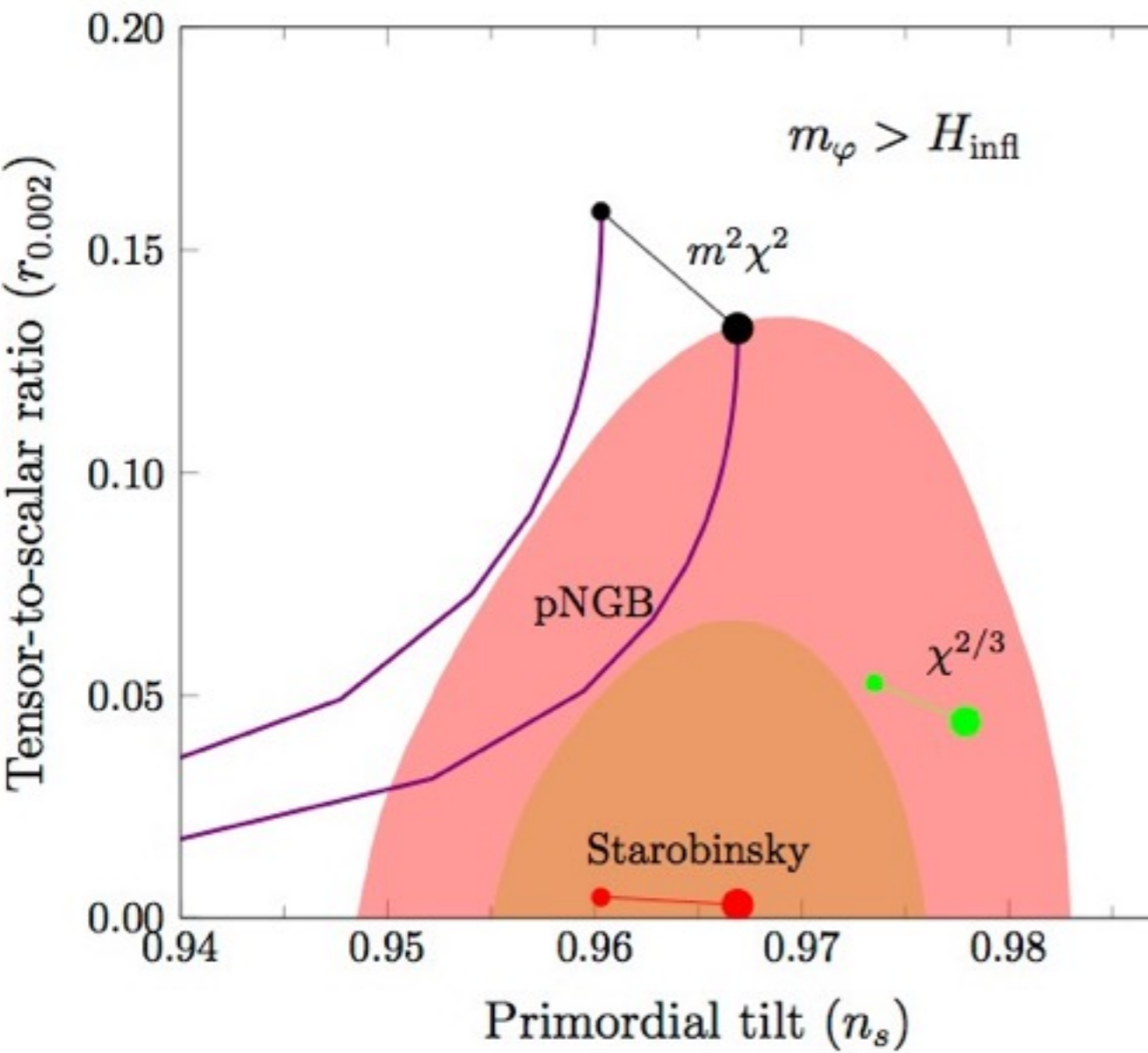
$$\begin{aligned} & \frac{1}{6} \ln \left(\frac{16\pi M_{Pl}^2 Y^4}{m_\varphi^2} \right) + \frac{1}{4} (1 - 3w_{rh1}) N_{re1} + \frac{1}{4} (1 - 3w_{rh2}) N_{re2} \\ & = 55.43 - N_{inf} + \frac{1}{4} \ln r + \frac{1}{4} \ln \left(\frac{\rho_k}{\rho_{end}} \right) \end{aligned}$$

Conclusions

- modulus dominated cosmology is a generic feature of string/sugra motivated scenario

$$\hat{N}_{inf} = 55 - \frac{1}{3} \left(\frac{\sqrt{16\pi} M_{Pl} Y^2}{m_\varphi} \right)$$



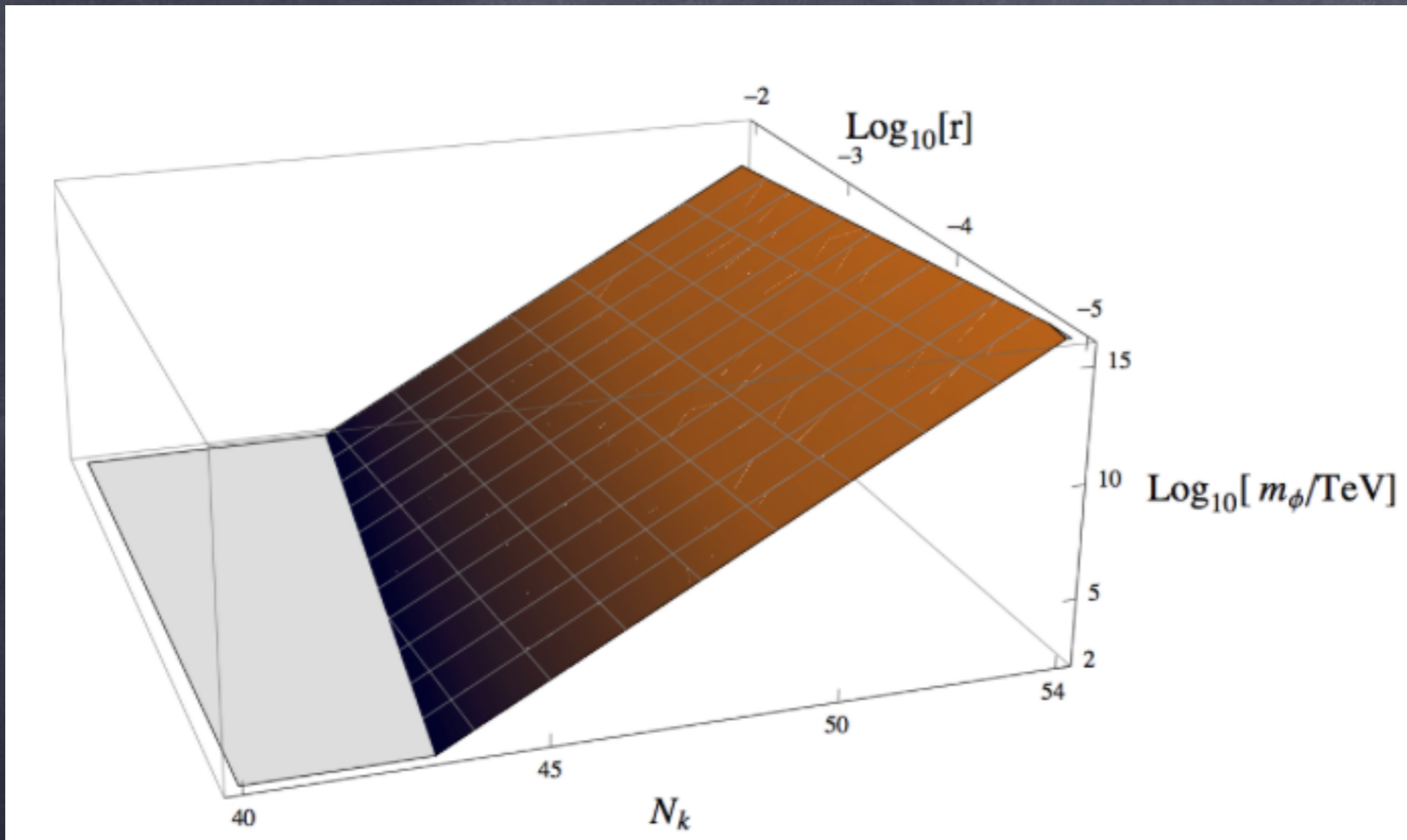


Das, Maharana, K.D

sensitivity $n_s \sim 10^{-3}$

DECIGO/PRISM/21 Cm

Bound.



for $N > 44.5$,
the bound
much
stronger than
BBN bound

Fibre Inflation: $r < 0.01$ and $N > 50$ for CMB observations

Strong bound for chaotic inflation

Insignificant for monodromy models ..

Conclusions

- modulus dominated cosmology is a generic feature of string/sugra motivated scenario

$$\hat{N}_{inf} = 55 - \frac{1}{3} \left(\frac{\sqrt{16\pi} M_{Pl} Y^2}{m_\varphi} \right)$$



- Independent constraint on modulus mass derived using precision CMB data

Thank You